

Model Population Analysis

(模型集群分析)



Hong-Dong Li and Yi-Zeng Liang

lhdcslu@gmail.com

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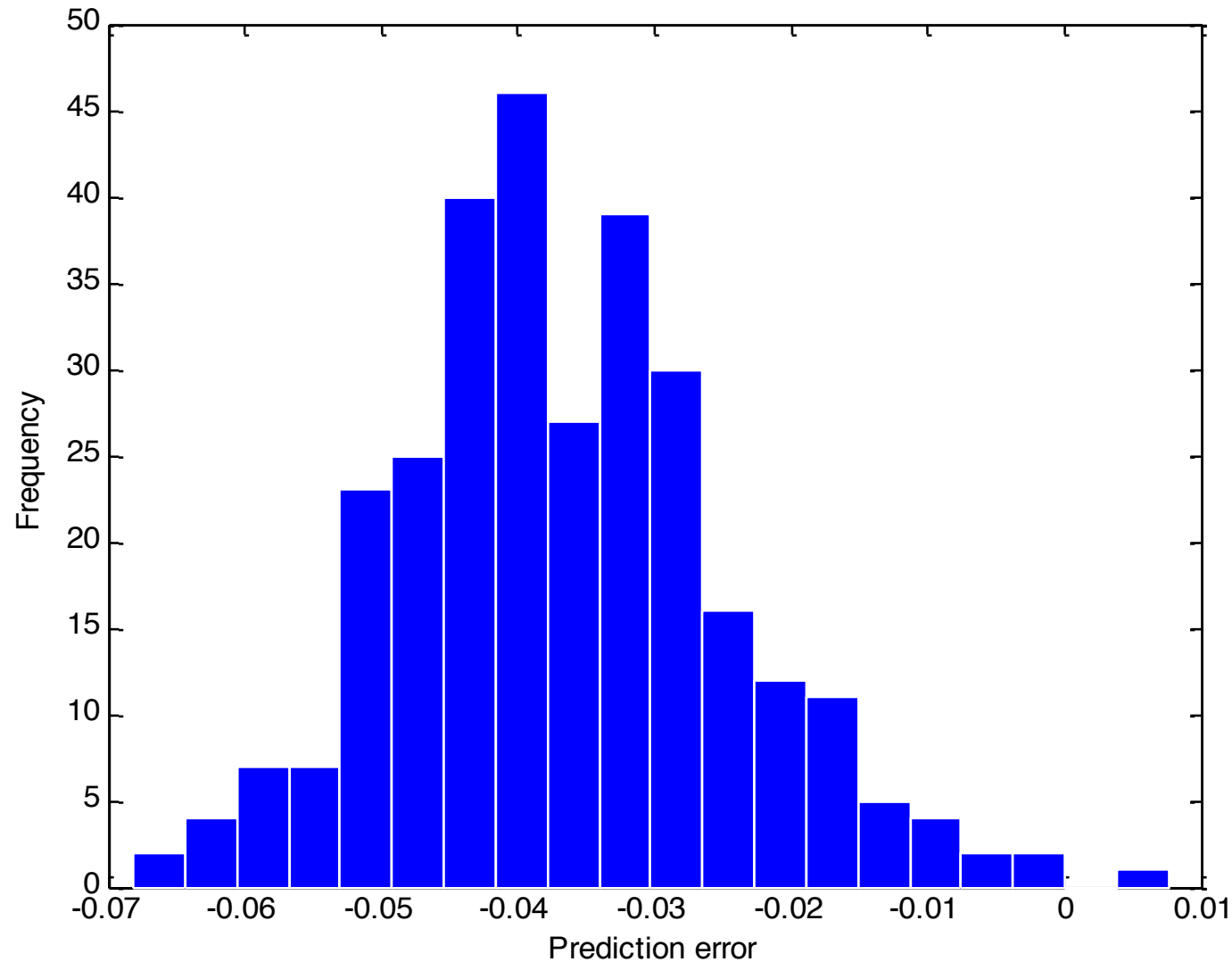
Outline

- **Context**
- **Model population analysis (MPA)**
- **Variable assessment using MPA**

Context

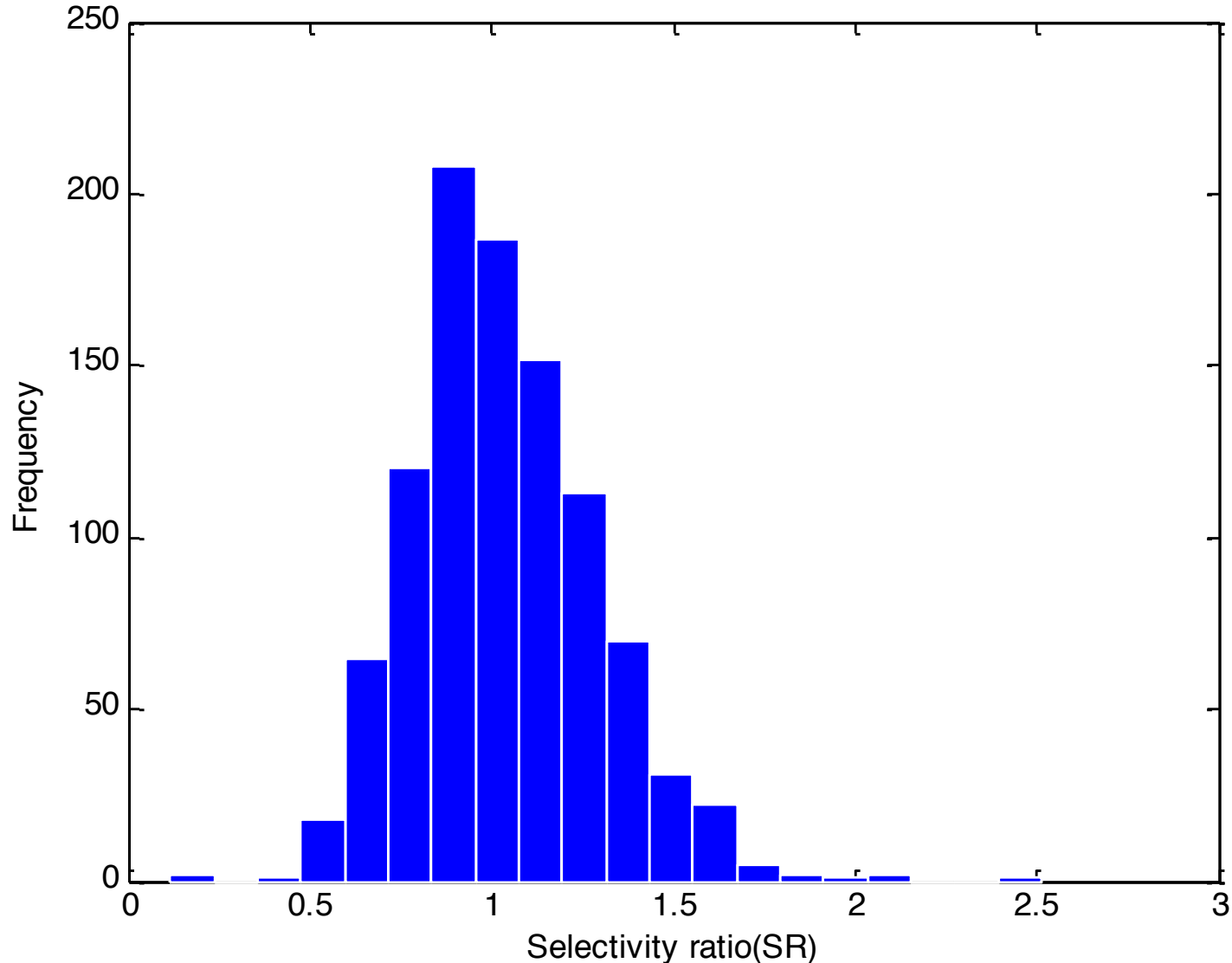
- ❖ Outlier detection
- ❖ Variable assessment
- ❖ Model performance
- ❖ Ensemble learning

Outlier



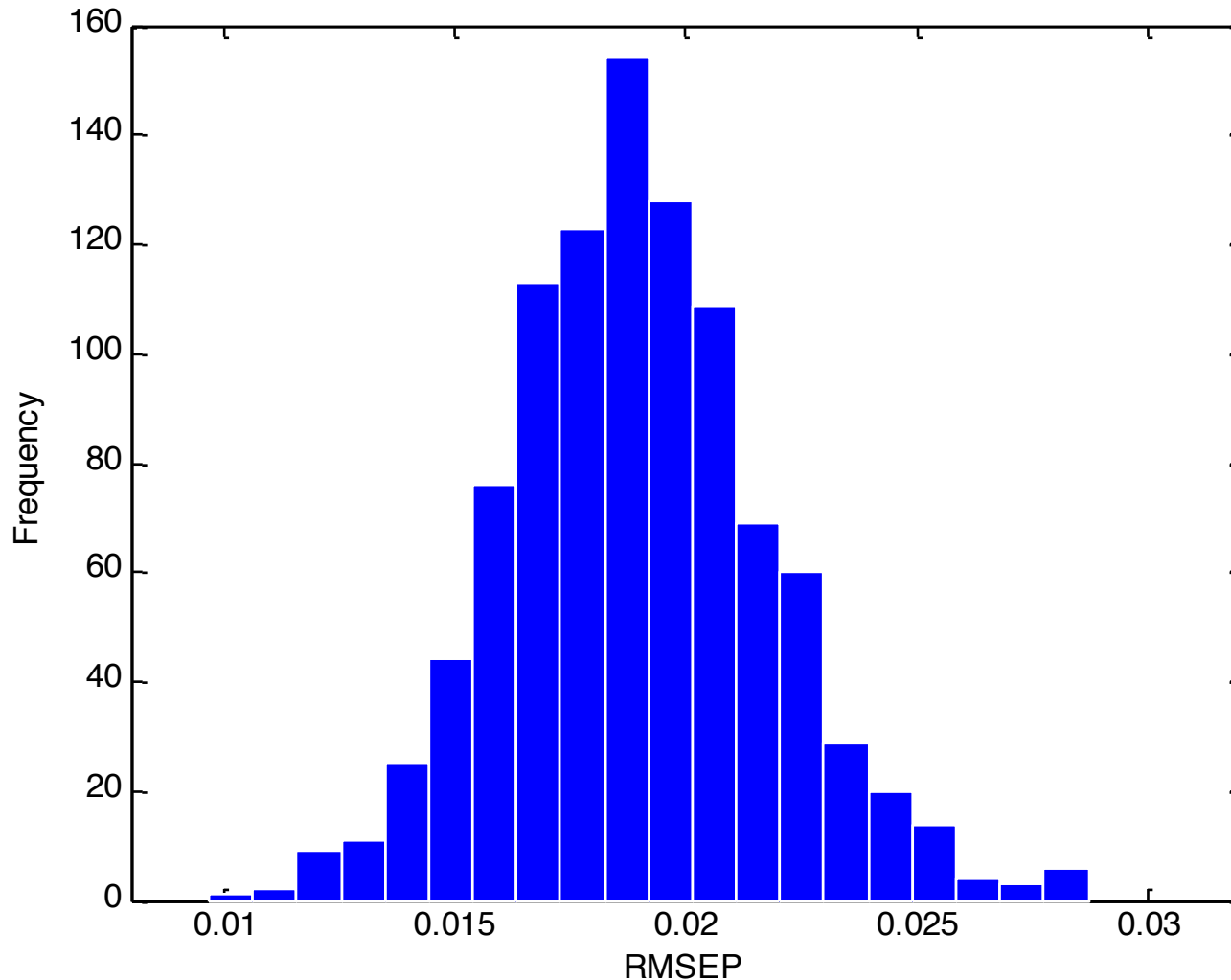
Corn data: Prediction errors of a test sample **from 303 models**

Variable importance



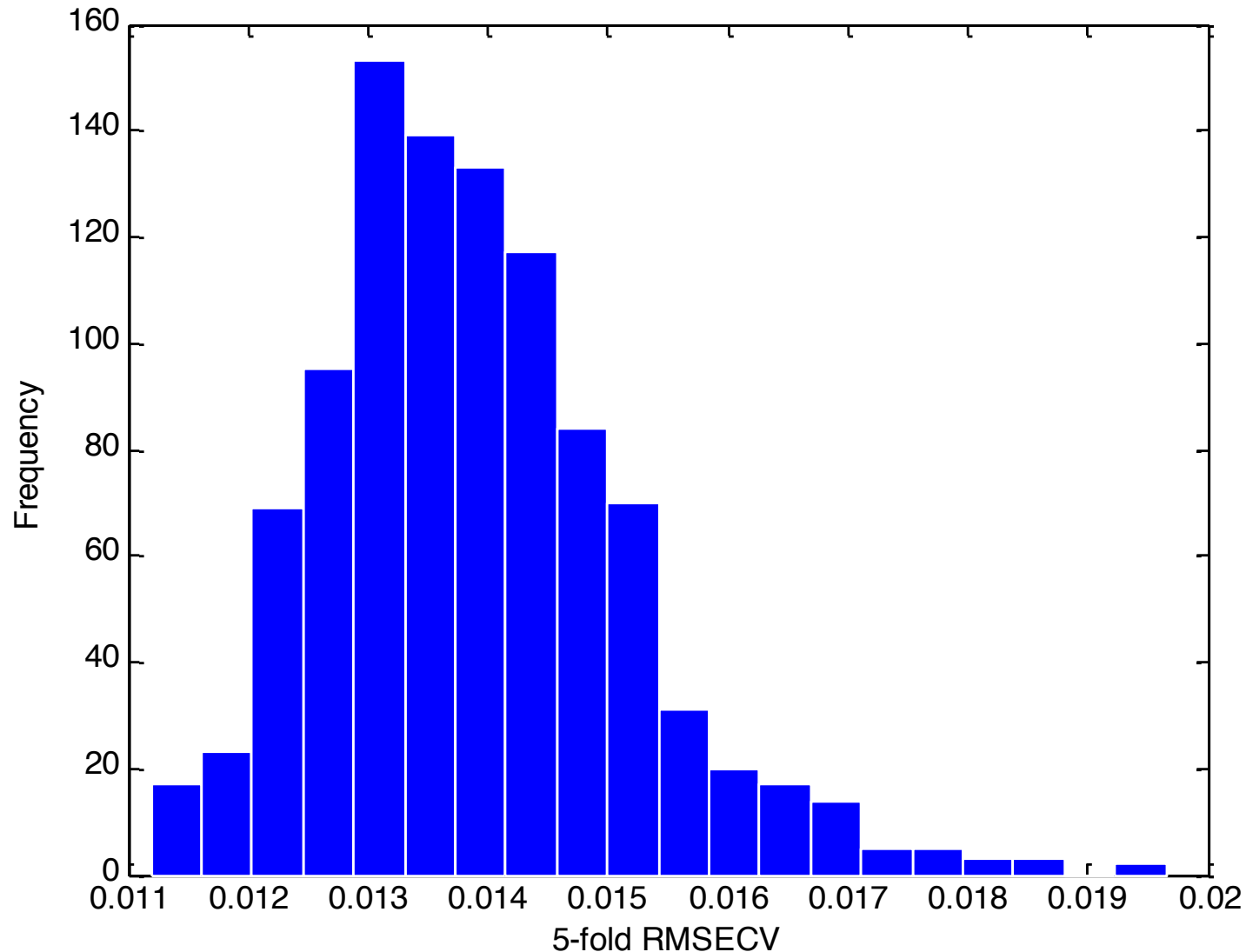
T2DM data (n=90, p=21), 70% samples, **from 1000 models**

Model performance: test set



Data: corn m5 moisture. **From 1000 models**

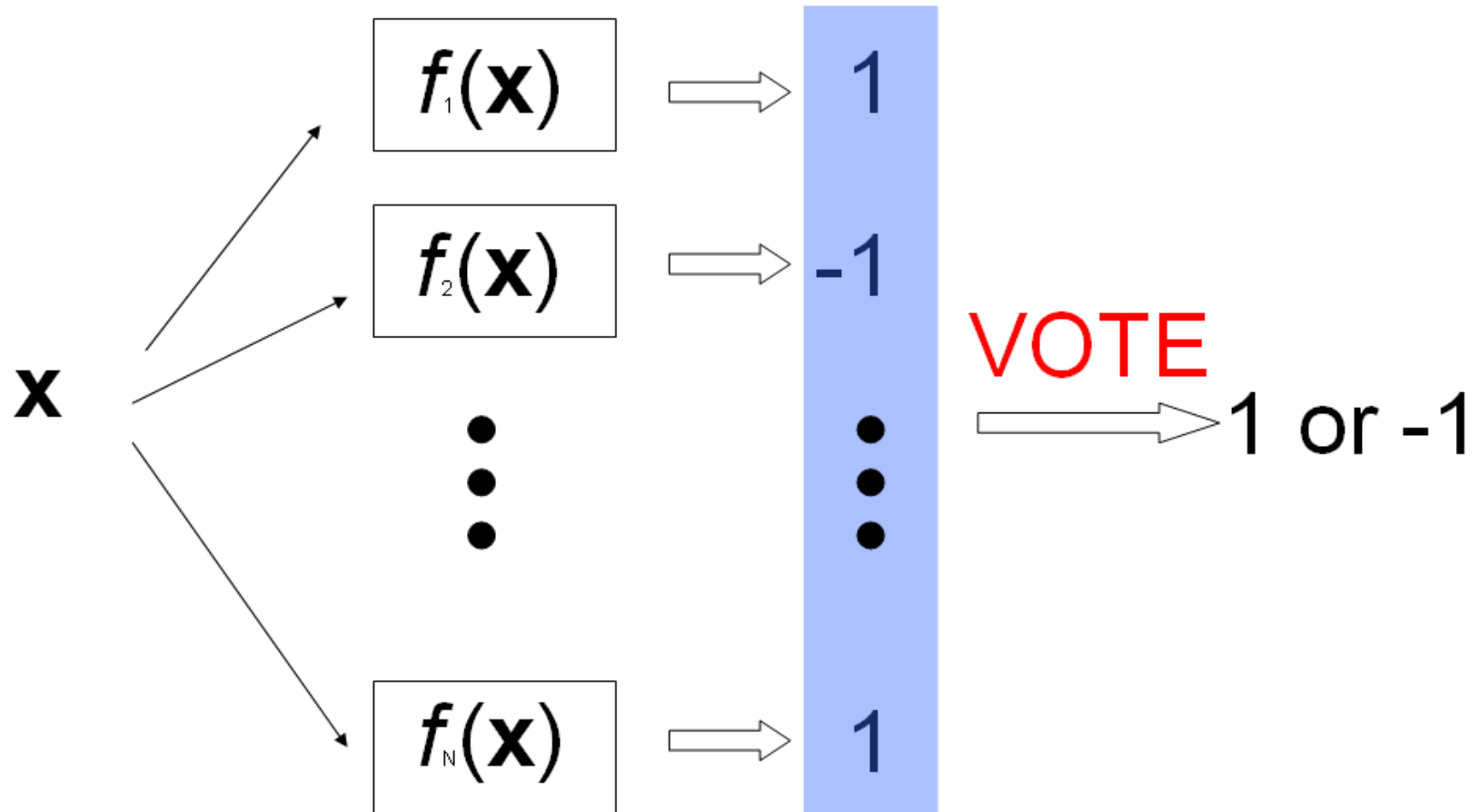
Model performance: cross validation



Data: corn m5 moisture. **From 1000 models**

Ensemble learning

Bagging, Boosting and Random forest



A population of **N models**

Conclusions

- ◆ Prediction errors or variable importance or model performance is **data-dependent**
- ◆ A **single number** is not sufficient to characterize...
- ◆ Hence we suggest to use the **distribution** of ...

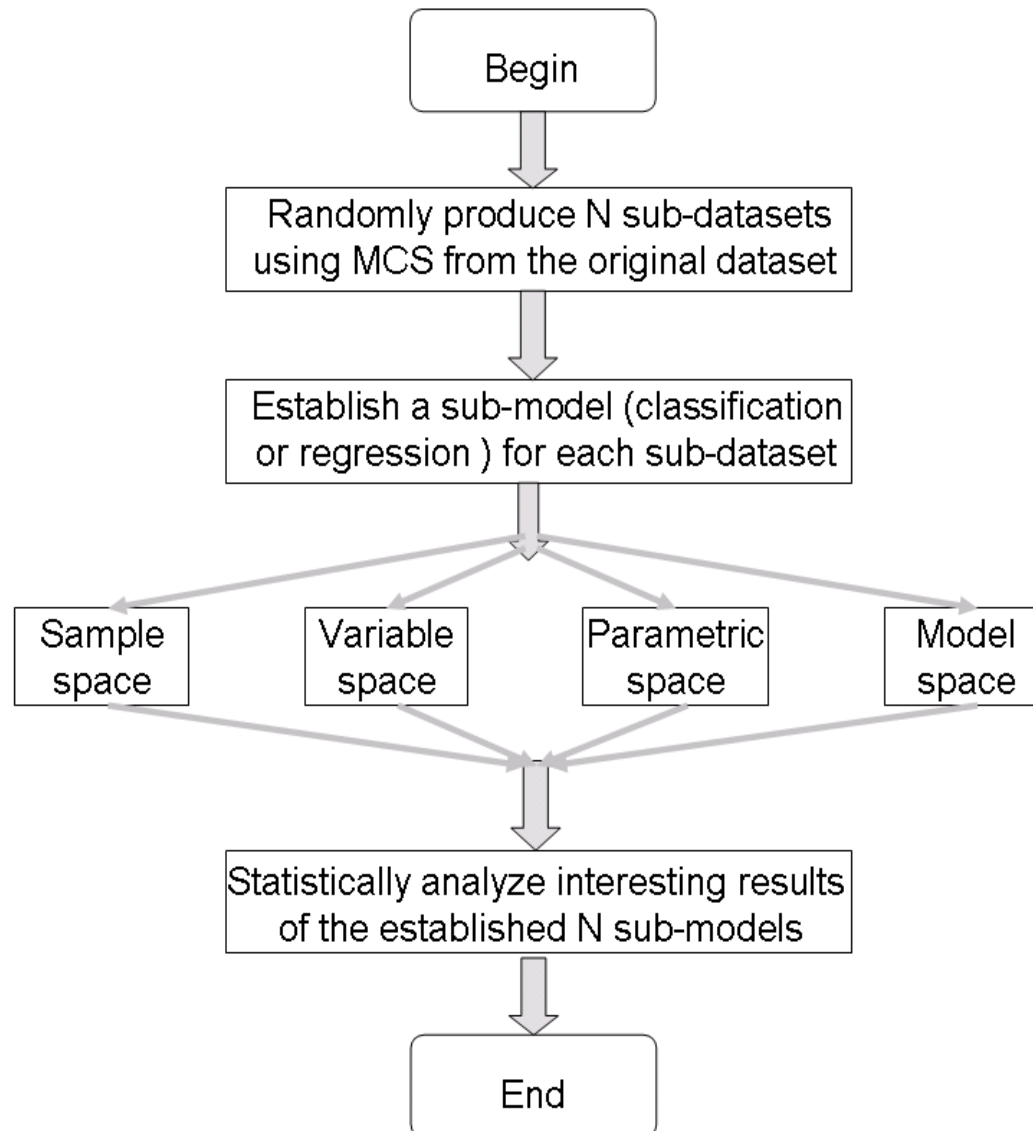
A new concept

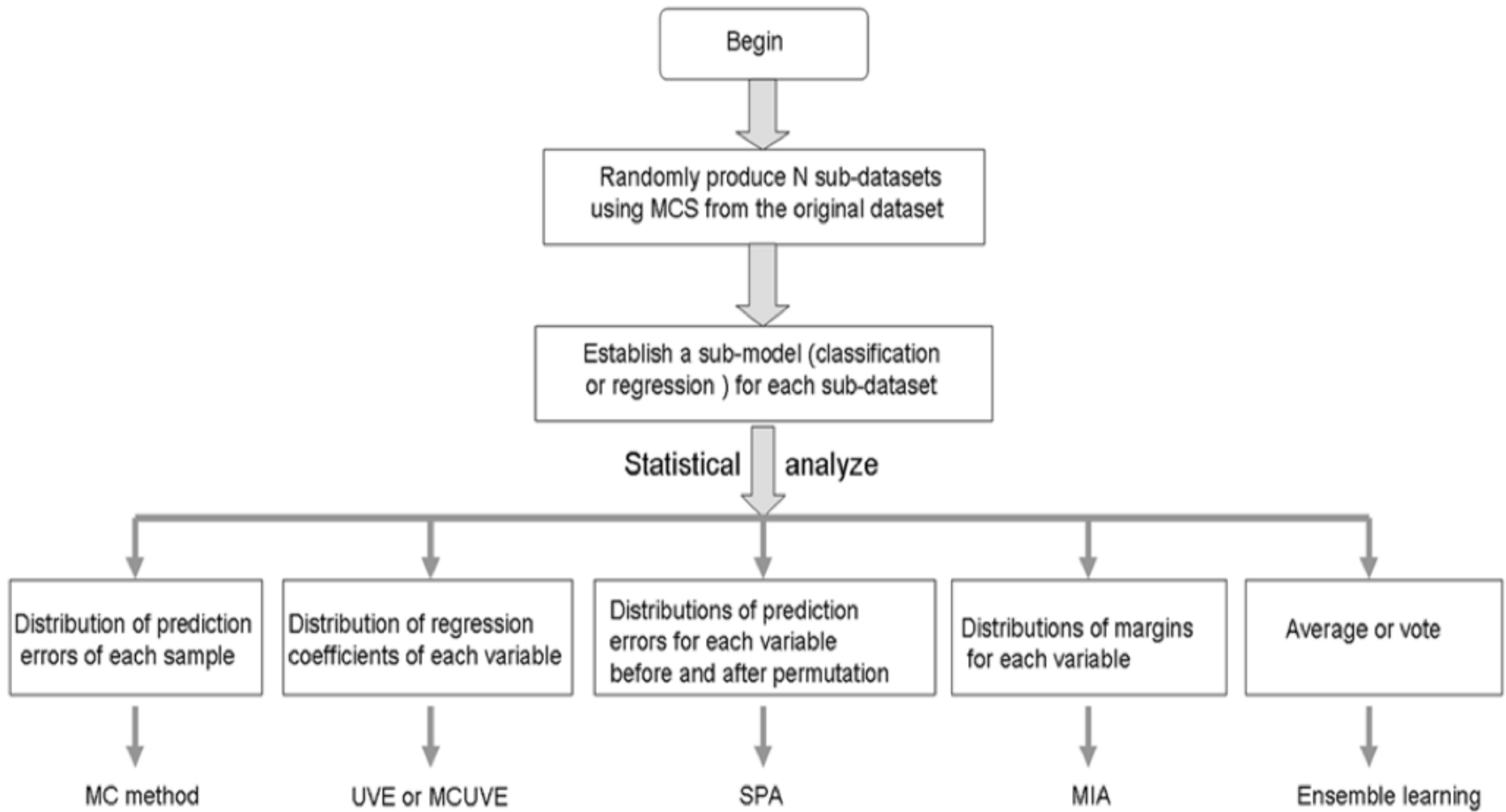
Model Population Analysis

Hong-Dong Li, Yi-Zeng Liang, Qing-Song Xu, Dong-Sheng Cao, model population analysis for variable selection, *Journal of Chemometrics* **2009**, 24, (7-8), 418-423

What is Model Population Analysis?

A general framework for developing data analysis methods





Our work on **model population analysis**

- [1]. Li, H.-D., Liang, Y.-Z., Xu, Q.-S. & Cao, D.-S. Model population analysis for variable selection. *Journal of Chemometrics* 24, 418-423 (2009).
- [2]. Cao, D.S., Liang, Y.Z., Xu, Q.S., Li, H.D. & Chen, X. A New Strategy of Outlier Detection for QSAR/QSPR. *J. Comput. Chem.* 31, 592-602 (2010).
- [3]. Li, H.-D. et al. Recipe for revealing informative metabolites based on model population analysis. *Metabolomics* 6, 353-361 (2010).
- [4]. Li, H.-D. et al. Recipe for Uncovering Predictive Genes using Support Vector Machines based on Model Population Analysis, <http://doi.ieeecomputersociety.org/10.1109/TCBB.2011.36>. *IEEE/ACM Transactions on Computational Biology and Bioinformatics* (2011).
- [5]. Wang, Q., Li, H.-D., Xu, Q.-S. & Liang, Y.-Z. Noise incorporated subwindow permutation analysis for informative gene selection using support vector machines. *Analyst* 136, 1456-1463 (2011).
- [6]. Li, H.-D., Liang, Y.-Z. & Xu, Q.-S, Model population analysis and its applications in chemical and biological modeling, *under review*
- [7]. Li, H.-D., Liang Y.-Z&Xu, Q.-S, Variable complementary network: a novel approach for identifying disease related variables and their mutual associations, in preparation
- [8]. Li, H.-D., Liang Y.-Z&Xu, Q.-S, statistical model comparison via model population analysis, an invited book chapter, *under review*

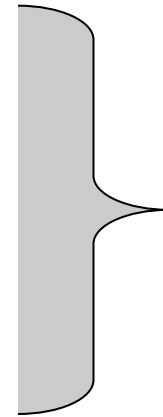
How to implement MPA?

1. Monte Carlo Sampling
to obtain **sub-datasets**

Monte Carlo Sampling

- Jackknife

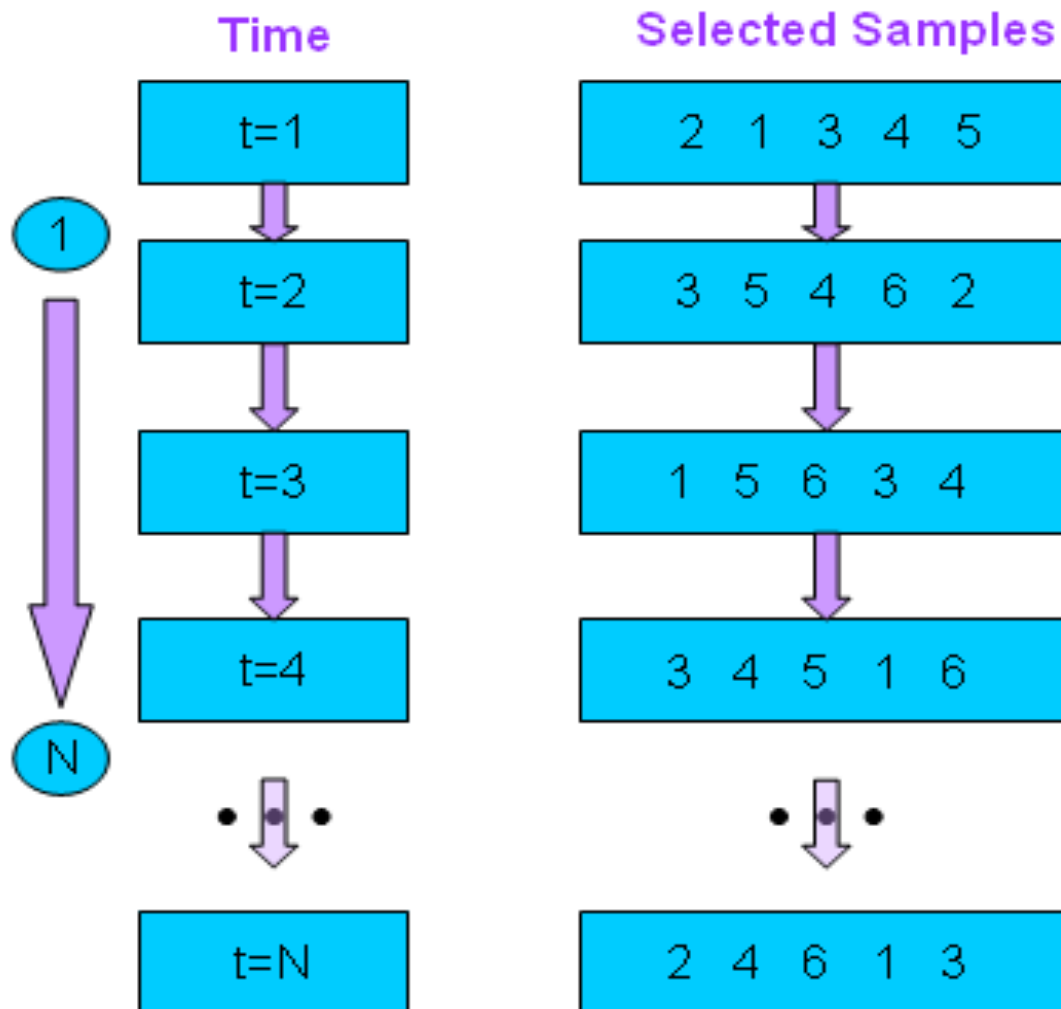
- Bootstrap



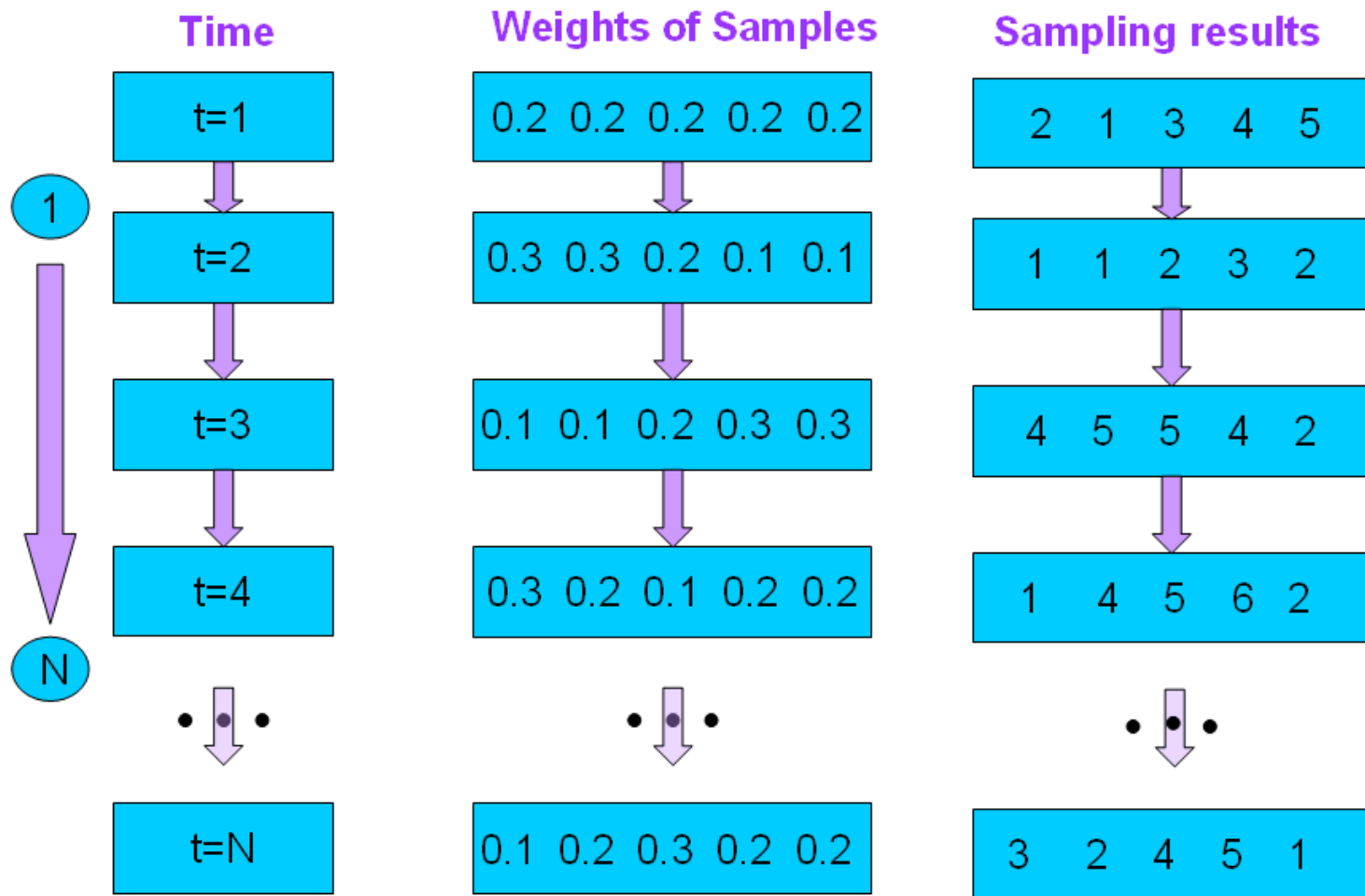
Reweighted version

Jackknife

---Suppose we have 6 samples, denoted by 1, 2, 3, 4, 5 and 6



Weighted sampling



Suppose we have 5 samples, denoted by 1, 2, 3, 4 and 5

2. Build N sub-model for all **N sub-datasets**

Partial least squares

Support vector machines

Classification And Regression Trees

...

3. Statistical analysis of an **interesting output** of all the N sub-models

- ◆ Prediction residual of a sample
- ◆ Regression coefficient of a variable
- ◆ Variable importance
- ◆ Model-related parameter
- ◆ ...

Model Population Analysis for **variable assessment**

Three new algorithms based on MPA:

SPA: Subwindow Permutation Analysis

MIA: Margin Influence Analysis

CIMPA: Conditional importance

To illustrate that:

Different kinds of designs for statistical analysis of some interesting parameters will result in different algorithms.



Subwindow Permutation Analysis

Motivated by:

- **Random forest**
- **Model Population Analysis**
- **Detecting synergistic effect**

HD Li, MM Zeng, BB Tan, YZ Liang, QS Xu, DS Cao, Recipe for revealing informative metabolites based on model population analysis, *Metabolomics* **2010**, 6, (3), 353-361.

What is permutation?

ID	normal	permuted	permuted
1	0.75	0.47	0.53
2	0.67	0.02	0.20
3	0.20	0.45	0.85
4	0.93	0.85	0.02
5	0.53	0.93	0.67
6	0.42	0.67	0.93
7	0.45	0.75	0.42
8	0.85	0.42	0.47
9	0.47	0.20	0.45
10	0.02	0.53	0.75

Lindgren, F., Hansen, B., & Karcher, W. (1996). Model validation by permutation tests: Applications to variable selection. *Journal of Chemometrics*, 10, 521–532.

Variable importance in Random Forest (RF)

$\text{Error_normal} = \text{RF}(\text{Xtest})$

$\text{Error_permuted} = \text{RF}(\text{Xtest}_j)$

$\text{Variable importance}_j = \text{Error_permuted} - \text{Error_normal}$

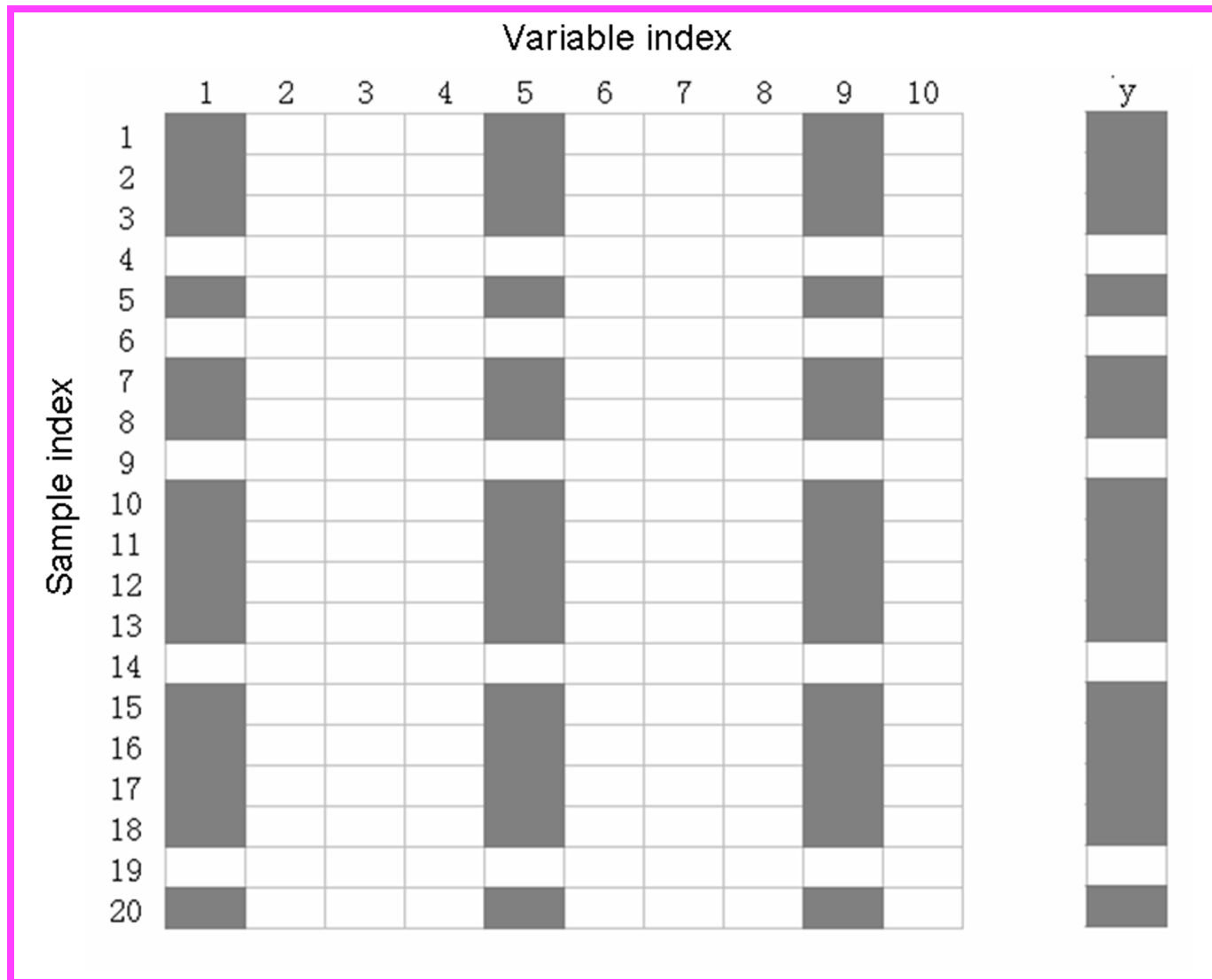
Breiman, L. (2001). Random forests. *Machine Learning*, 45, 5–32.

SPA is developed

by exactly following the three elements of
MPA

- (1) sub-dataset sampling (N)
- (2) sub-model building (N)
- (3) statistical analysis of the interesting parameters of all the N models.

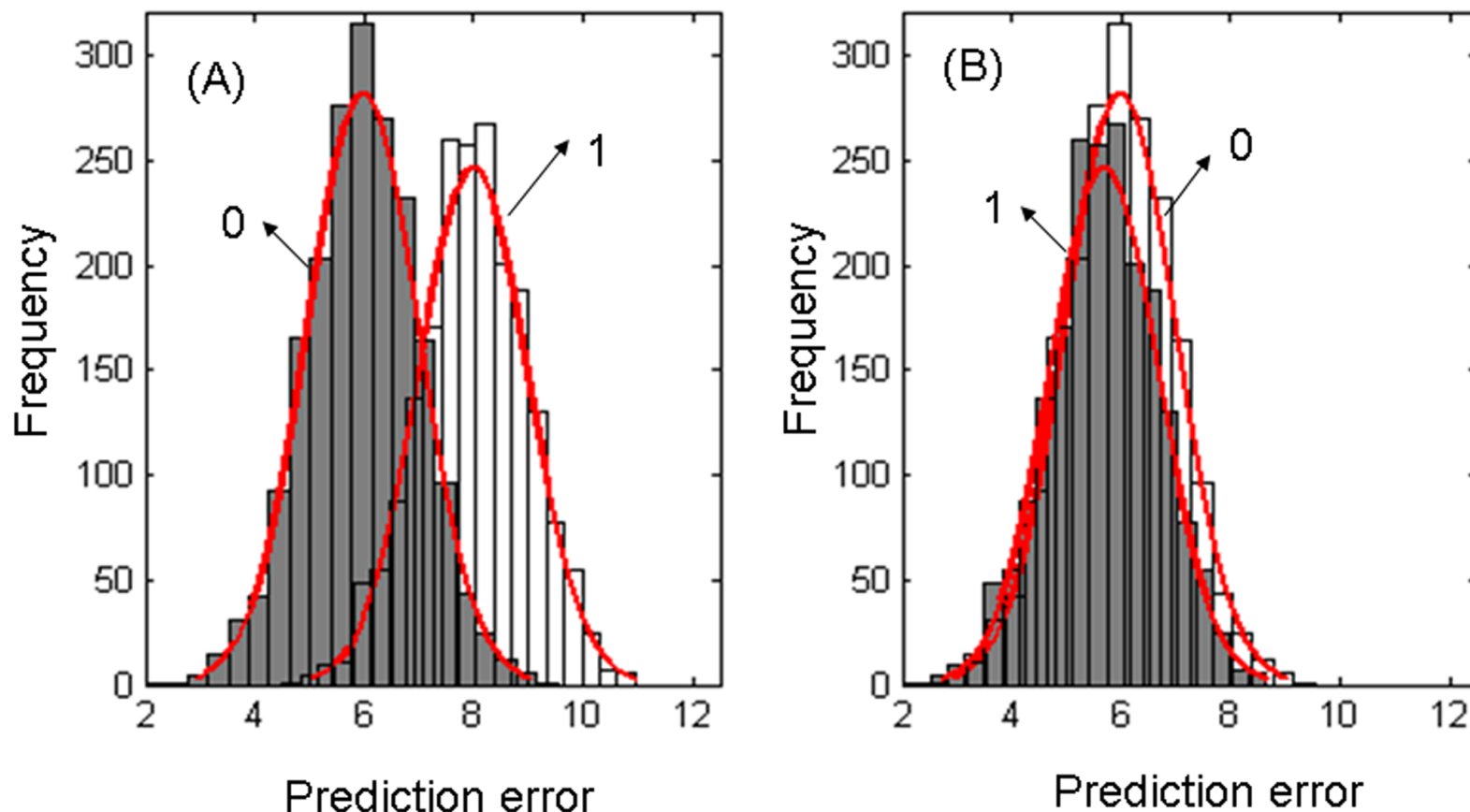
1. Sub-dataset sampling



2. Build N sub-models

ID	variable			Model	Test set	Prediction on test sets			
1	1	3	5	M1	Xtest1	NPE	PPE1	PPE3	PPE5
2	7	2	6	M2	Xtest2	NPE	PPE7	PPE2	PPE6
3	9	1	10	M3	Xtest3	NPE	PPE9	PPE1	PPE10
.			
N	6	4	8	MN	XtestN	NPE	PPE6	PPE4	PPE8

3. Statistical analysis of the prediction errors of the N sub-models



Peak 1: Permuted prediction errors (PPEs)

Peak 0: Normal prediction errors (NPEs)

How to compare the paired distributions?

**We use the nonparametric
Mann-Whitney U test**

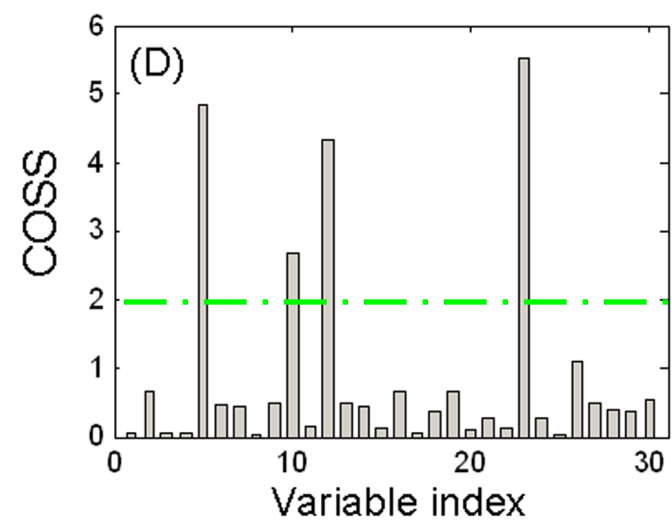
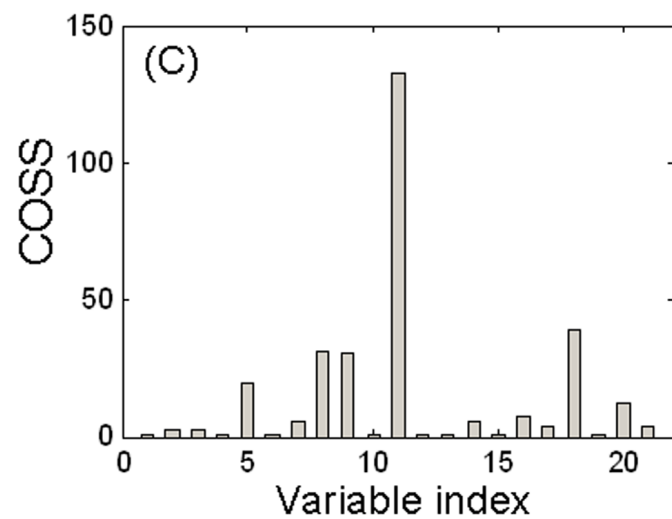
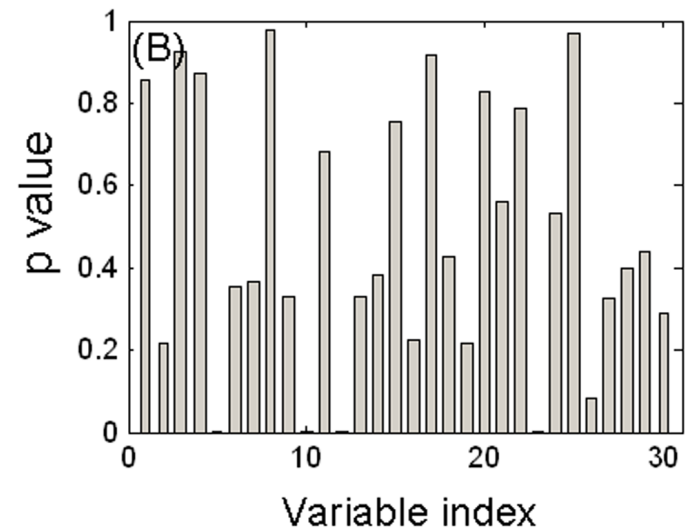
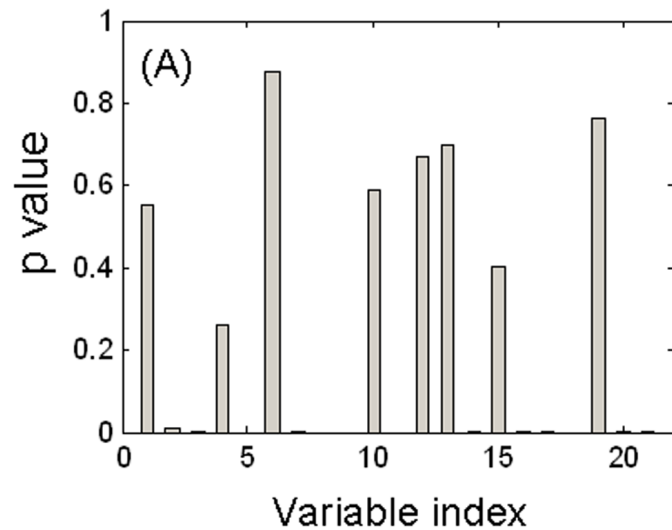
Lead to a COnditional Synergistic Score: **COSS**

$$\text{COSS} = -\text{Log}_{10}(p)$$

Applications of SPA to

- Type 2 diabetes mellitus data
- Childhood overweight data

Source codes in MATLAB and R can be freely available at <http://code.google.com/p/spa2010>



SPA-based Conditional P-value and the **COSS** score

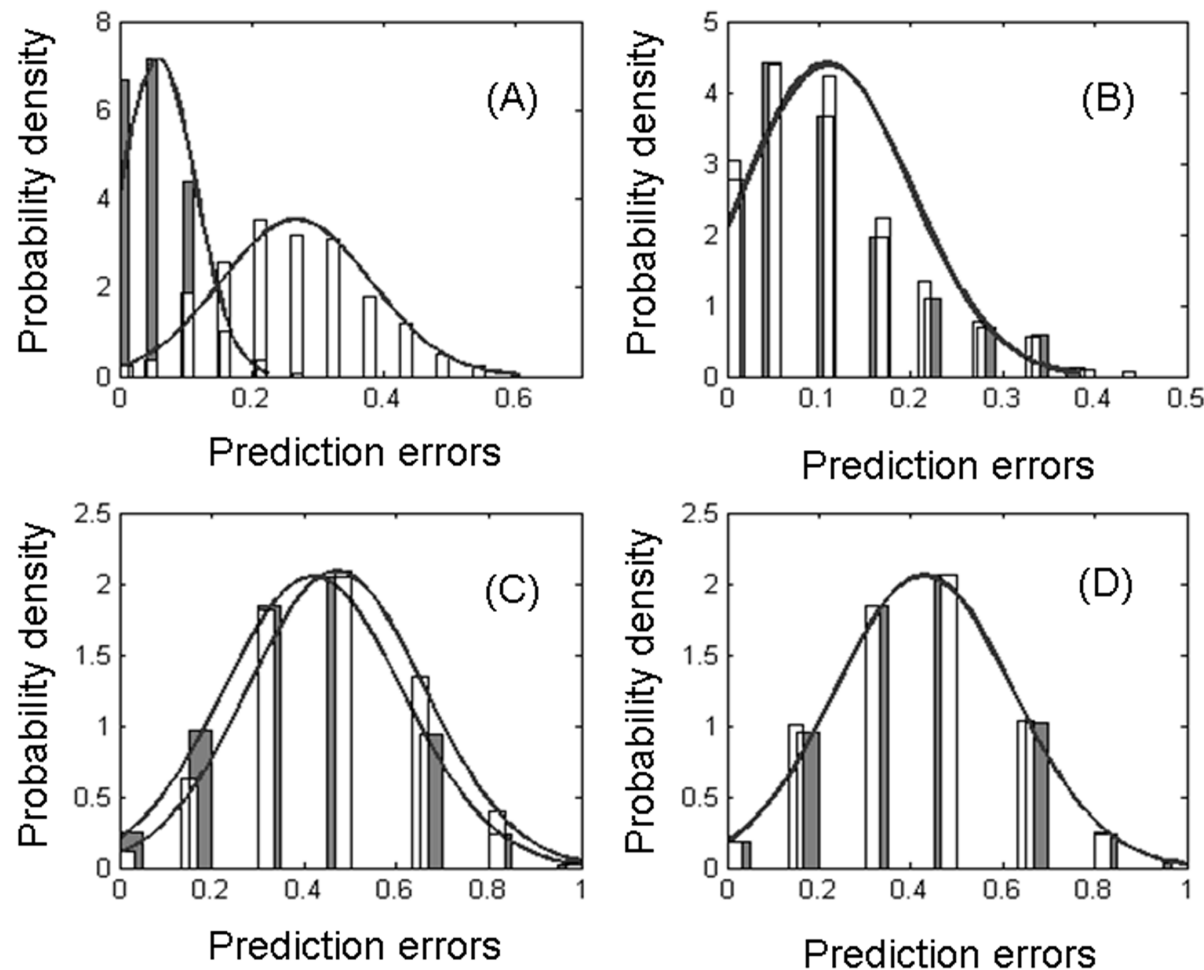


Fig. 4 Plot **A** and **B** shows the distributions of normal prediction errors (*grey bar*) and permuted prediction errors (*white bar*) of an informative metabolite (C18:1n-9, $p = 0$) and an uninformative one (C16:1n-7, $p = 0.8791$) for T2DM data, respectively. By analogy, such kind of distributions of an informative metabolite (Palmitic acid, $p = 3 \times 10^{-6}$) and an uninformative one (Leucine, $p = 0.9791$) for the childhood overweight data are shown in Plot **C** and **D**, respectively

Compare two distributions

Unsupervised

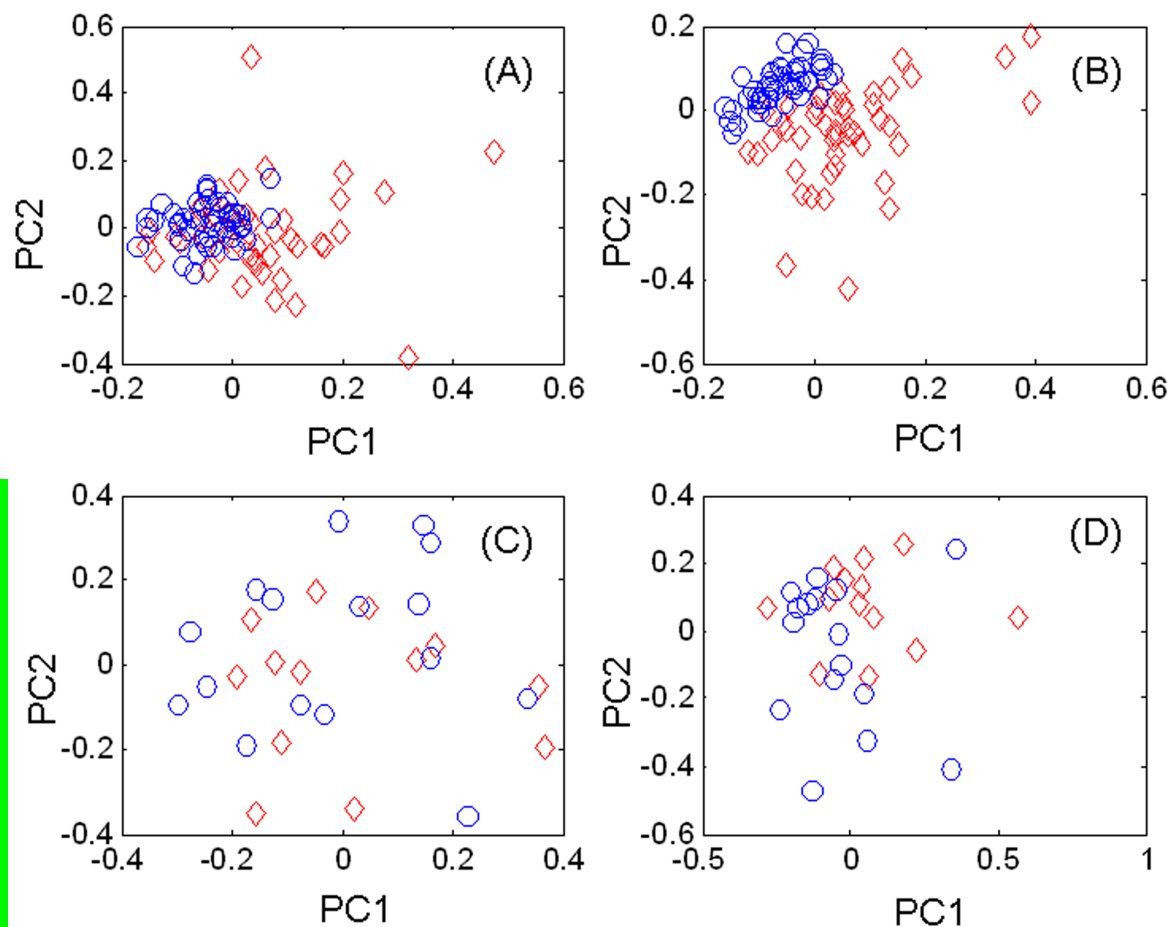


Fig. 5 Plot A and B display the PCA projected samples (*circle*: normal, *diamond*: patients) of the T2DM data using all the 23 metabolites and the selected three metabolites by SPA, respectively. Analogously, Plot C and D display the PCA projected samples (*circle*: normal, *diamond*: overweight) of the childhood overweight data using all the 30 metabolites and the selected three metabolites by SPA, respectively

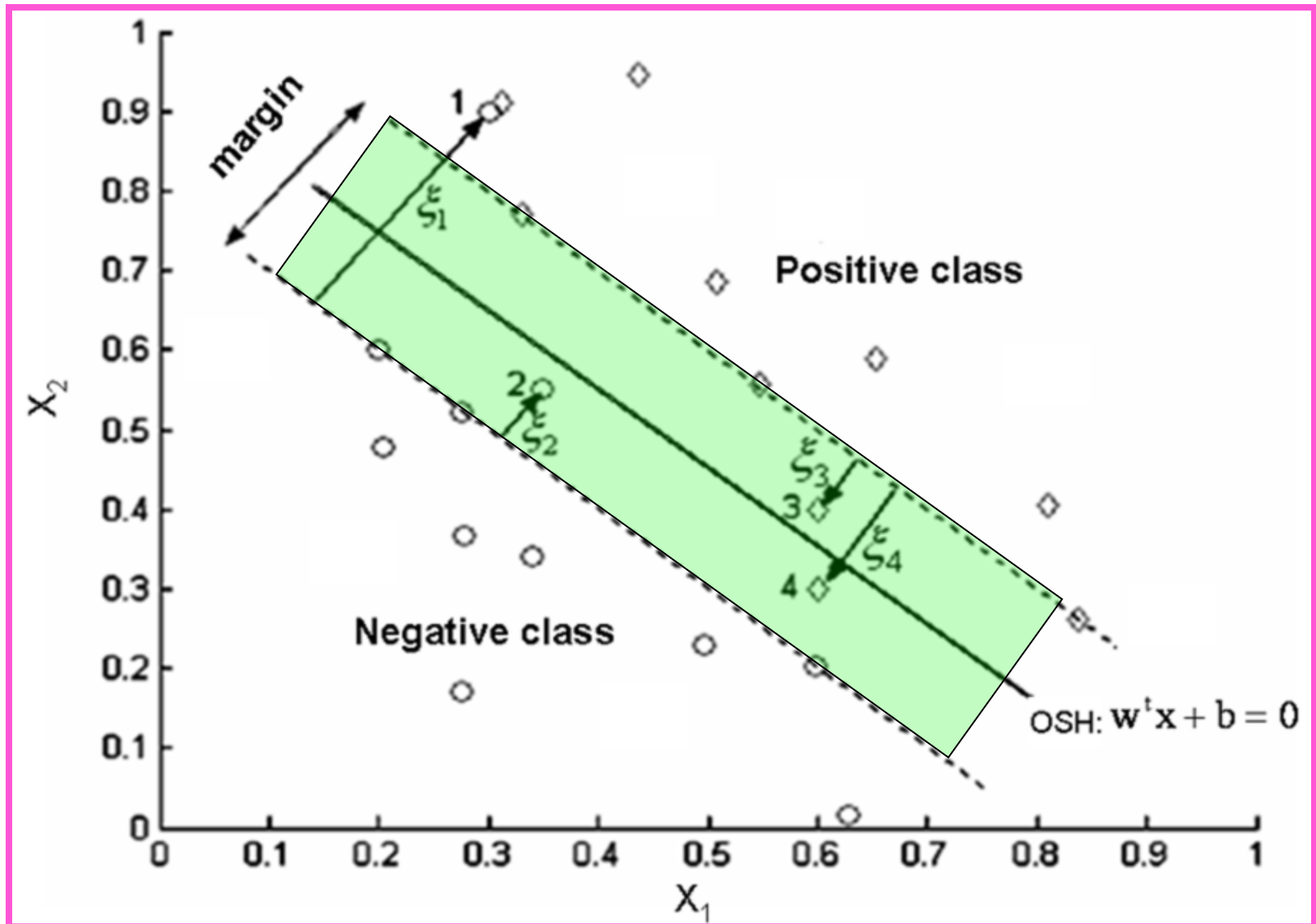
Better separation

Margin Influence Analysis

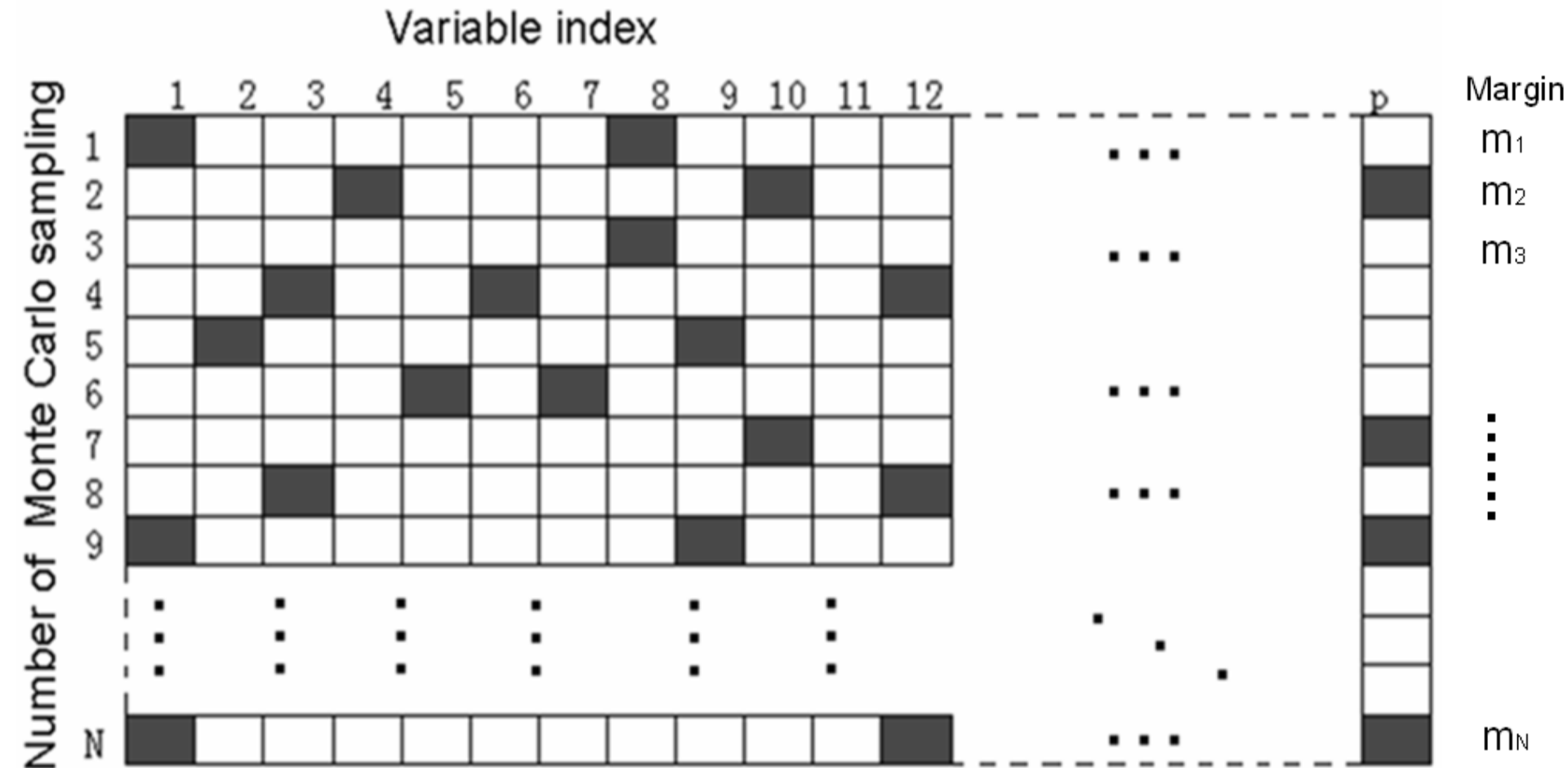


Hong-Dong Li, Yi-Zeng Liang*, Qing-Song Xu et al, Recipe for Uncovering Predictive Genes using Support Vector Machines based on Model Population Analysis, *IEEE/ACM Transactions on Computational Biology and Bioinformatics*, <http://doi.ieeecomputersociety.org/10.1109/TCBB.2011.36>

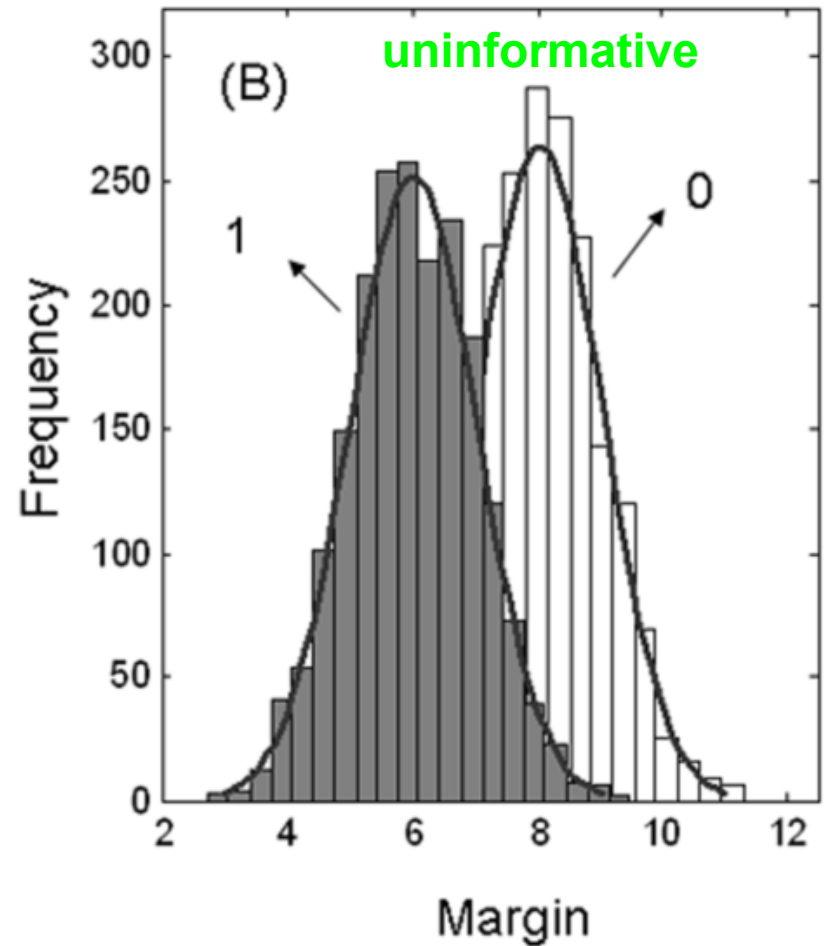
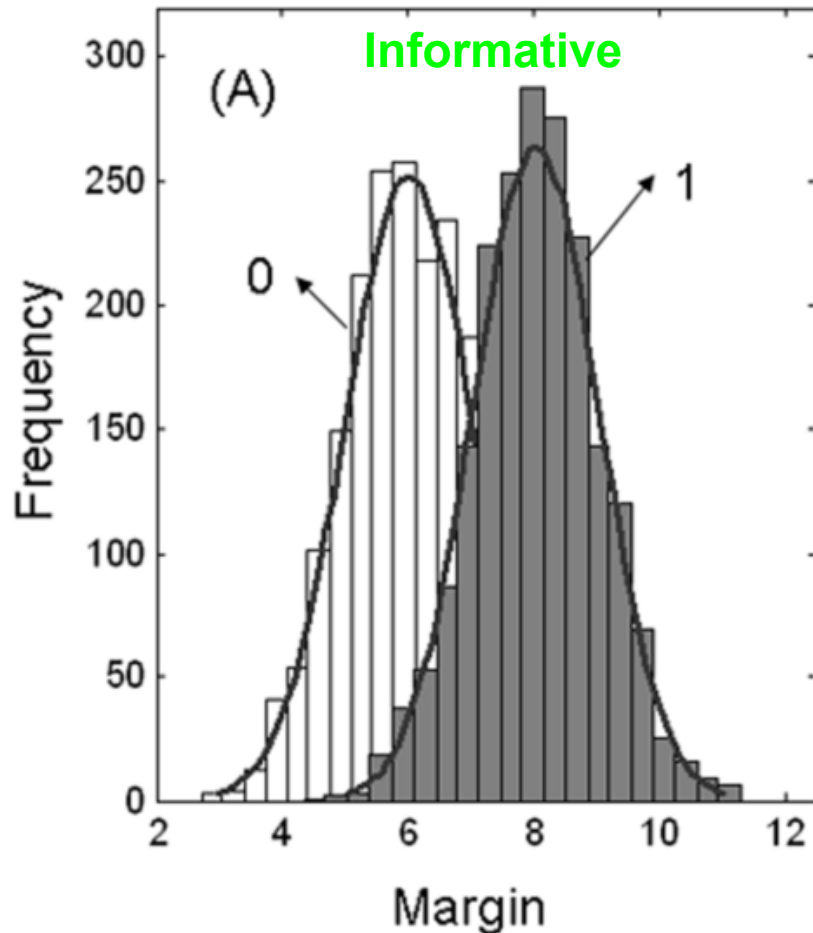
The margin of a SVM model



- 1 Sub-dataset sampling in variable space
- 2 Build N SVM models



3 Statistical analysis of the margin' s distribution

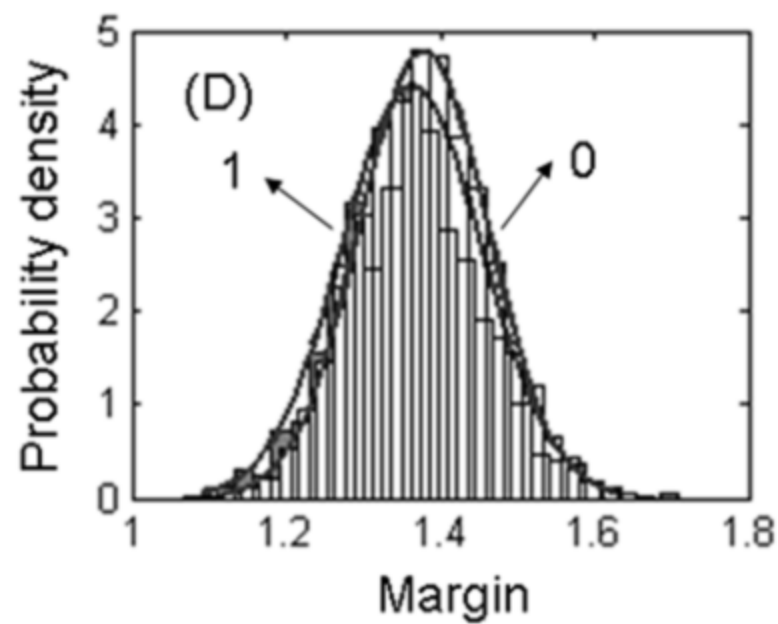
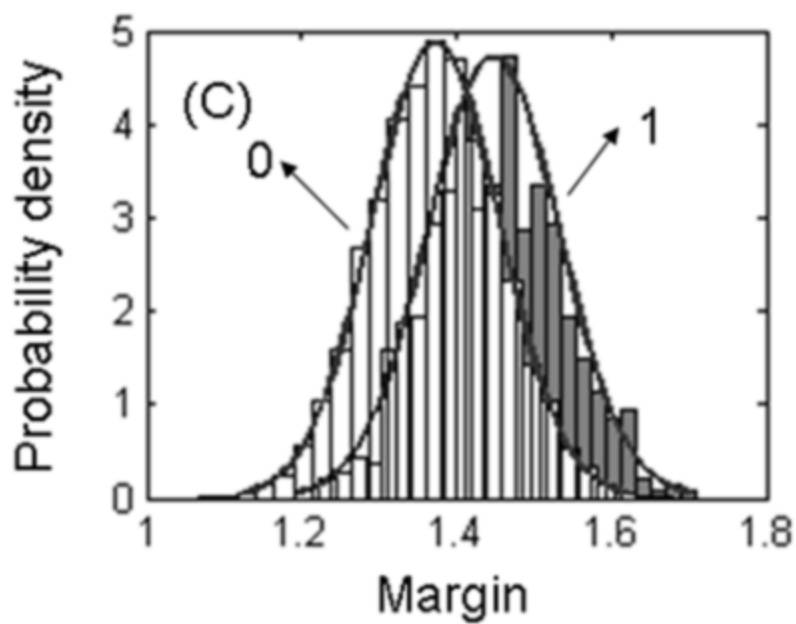
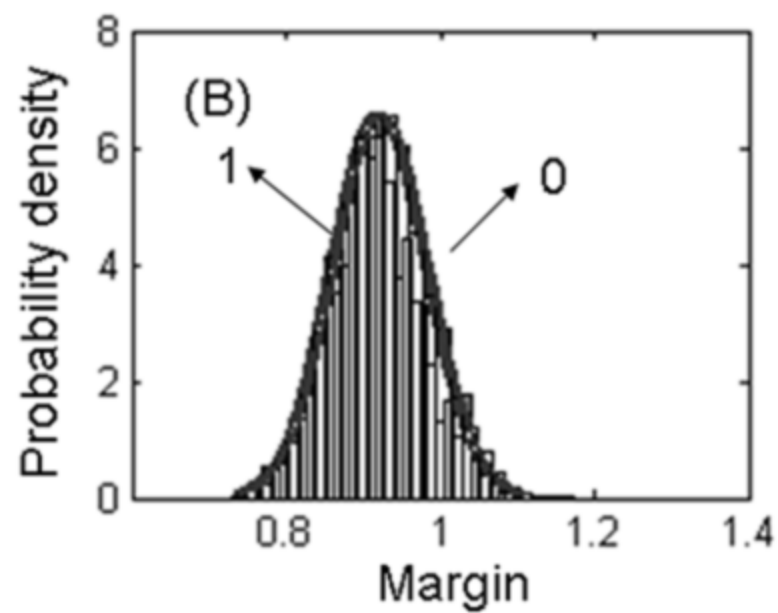
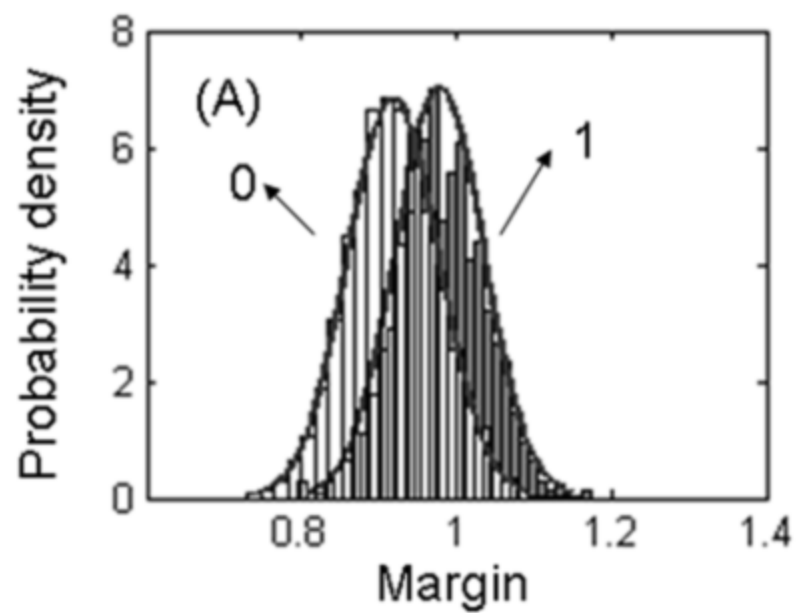


Peak 1: Margins of the Models with the variable included

Peak 0: Margins of the Models without the variable included

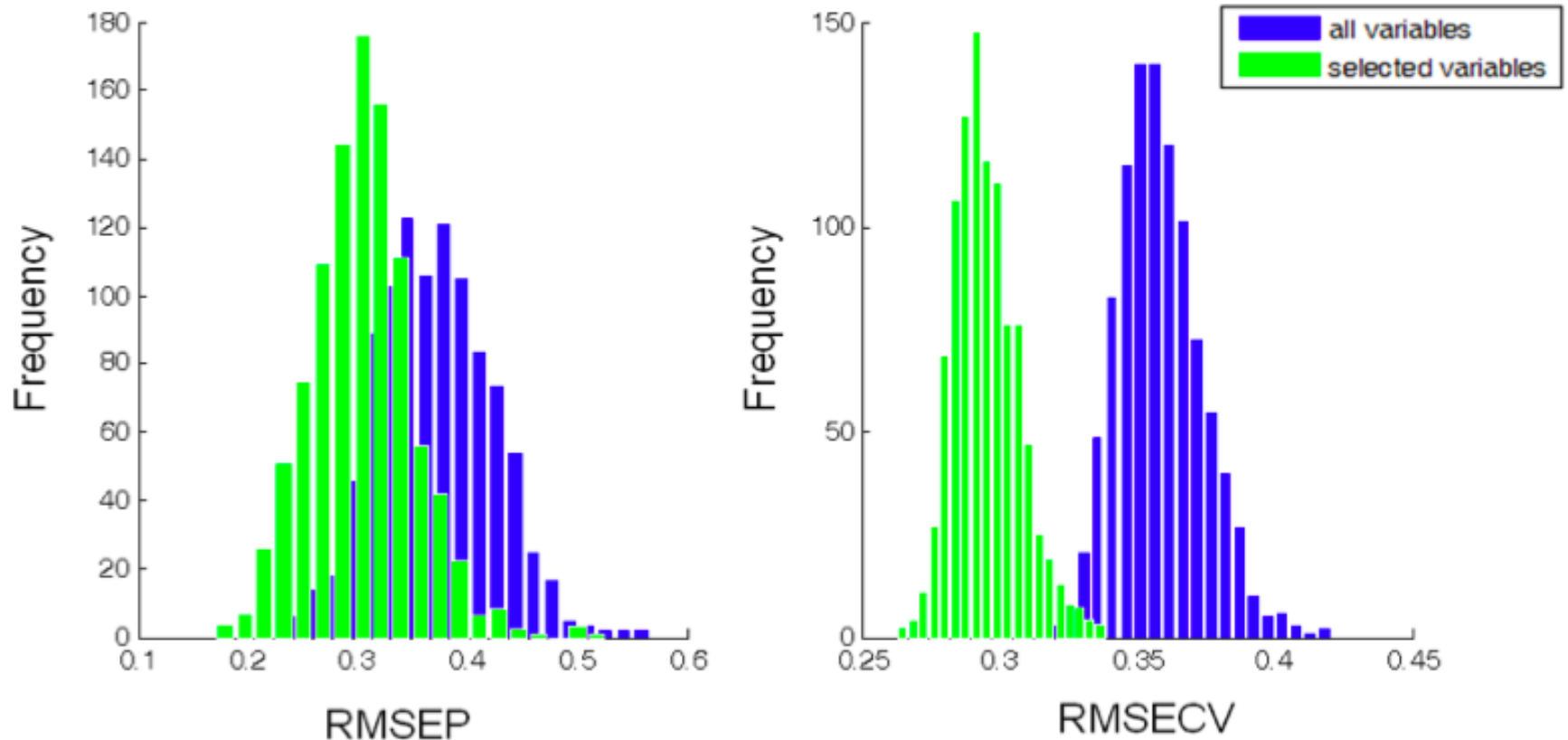
Applications

- **Colon data: 62 x 2000**
- **Estrogen data: 49 x 3333**



Model Assessment

Model assessment



Li, H.-D., Liang Y.-Z&Xu, Q.-S, statistical model comparison via model population analysis, **an invited book chapter, *under review***

Features of MPA-based methods:

- The computing process is **random**
- The final output is **stable**

For discussion?

- **Posterior distribution** from Bayesian analysis
- **Theoretical analysis** of MPA if possible?

Thank you very much



